A Comparison of ARIMA, Neural Network and Linear Regression

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Submission date: 29-Mar-2020 12:07AM (UTC+0700) Submission ID: 1283975510 File name: A_Comparison_of_ARIMA,_Neural_Network_and_Linear_Regression.pdf (389.48K) Word count: 3574 Character count: 15823 2010 Fourth Asia International Conference on Mathematical/Analytical Modelling and Computer Simulation

A Comparison of ARIMA, Neural Network and Linear Regression Models for the Prediction of Infant Mortality Rate

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Abstract—The aim of this paper is to compare the performances of ARIMA, Neural Network and Linear Regression models for the prediction of Infant Mortality Rate. The performance comparison is based on the Infant Mortality Rate data collected in Indonesia during the years 1995 – 2008. We com 5 re the models using performance measures such as Mean Absolute Error (MAE), Mean Absolute Percentage Error (MAPE) and Root Mean Square Error (RMSE). The results show that the Neural Network model with 6 input neurons, 10 4 dden layer neurons and using hyperbolic tangent activation functions for the hidden and output layers is the best among the different models considered.

Keywords: ARIMA, Neur 5 Network, Linear Regression, Infant Mortality Rate, Mean Absolute Error, Mean Absolute Percentage Error, Root Mean Square Error

I. INTRODUCTION

The infant mortality Rate (IMR) in a community is a widely used indicator of general health status. The IMR reflects a broad range of social, economic and medical conditions. Communities with problems such as unemployment, poverty, and low literacy tend to have higher infant mortality rates [1]. In Indonesia, the mortality statistic such as infant mortality is regarded as one of the important instruments to monitor and evaluate national health development.

The tim 51 ceries forecasting is employed in various applications to predict the futur 8 value using the past time series data. Many models have been applied in time series forecasting such as ARIMA, Logistic Regression and 86 ural Network. Choosing the best model is needed in the time series forecasting. These models have been used for different applications and from the result reported, it is clear that 46 performances of these models vary depending on the type of data used. In this paper, we present the performance comparison of these models for specific application, namely, prediction of IMR which is very useful for healthcare management. From this point of view, the result reported in this paper may be considered to be a significant contribution in the area of healthcare management.

The prediction or forecasting of IMR assumes importance for health departments since a good and accurate prediction is very helpful in devising appropriate action plans.

II. PREDICTION MODELS USED

This section describes the theory of the various models implemented in this paper.

A. ARIMA Model

Time series analysis has several objectives: modeling, forecasting and controlling. Forecasting deals with the issue of constructing models and methods that can be used to produce accurate short-term predictions [2]. The aim of modeling is to build a statistical model that adequately represents the long-term behavior of a time series. These goals are not necessarily identical. While the former frequently leads to a black box model that produces predictions, the objective of the latter is more towards finding the model **35** has generated the data.

A univariate time series $\{X_t\}$ is a series of observations of a variable over discrete intervals of time. These observations are equally spaced in time.

$$\{X_t\} = (x_1, x_2, x_3, ..., x_t)$$

The time series analysis involves modeling the series as a function 31 ts past observations and *errors* (*residuals*). Error (e_i) is the difference between the observed value (x_i) and the forecast value (\hat{x}_i):

$$e_t = x_t - \hat{x}_t \tag{2}$$

25 The two fundamental building blocks of a linear univariate time series model are the autoregressive (AR) model and moving average (MA) model. The forecast in AR

978-0-7695-4062-7/10 \$26.00 © 2010 IEEE DOI 10.1109/AMS.2010.20

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@computer society 18 del is a function of its past observations, while in a MA model the forecast is a function of its past errors.

An autoregressive model of order p, AR(p) is given by

$$\hat{x}_{t} = \phi_{1} x_{t-1} + \phi_{2} x_{t-2} + \dots + \phi_{p} x_{t-p}$$
(3)

A moving average model of order q, MA(q) is given by

$$\hat{x}_{t} = \theta_{1} e_{t-1} + \theta_{2} e_{t-2} + \dots + \theta_{q} e_{t-q}$$
(4)

The *order* of the model is defined by the highest term present in the describing equation. The order of an AR polynomial is denoted by p and that of a MA polynomial is denoted by q.

An autoregressive moving average (ARMA) process is a combination of autoregressive 10 and moving average polynomials in a single equation. An ARMA (p, q) model is defined by [3]:

$$x_{i} = \phi_{1}x_{i-1} + \phi_{2}x_{i-2} + \dots + \phi_{n}x_{i-p} + e_{i} + \theta_{1}e_{i-1} + \theta_{2}e_{i-2} + \dots + \theta_{q}e_{i-q}$$
(5)

where the orders of \overrightarrow{AR} and \overrightarrow{MA} polynomials are p and q respectively.

In order to make the notational form 22 ple, a special operator called the backshift operator (B) is used. The backshift operator is defined by

$$\frac{B^{j} x_{i} = x_{i-j}}{\text{where } j = 91, 2, \dots}$$
(6)

Finally, an ARMA (p, q) model can be expressed as

$$\phi(B)x_i = \theta(B)e_i \tag{7}$$

where $\phi(.)$ and $\theta(.)$ are the p^{th} and q^{th} degree polynomials are given by [4]:

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$$\phi(z) = 1 - \phi_1 z - \phi_2 z^2 - \dots - \phi_p z$$

and

$\theta(z) = 1 + \theta_1 z + \theta_2 z^2 + \dots + \theta_a z^q$

ARMA models c_{16} loyed for time series data using ordinary differencing are called autoregressive integrated moving average (ARIMA) models. In an ARIMA (p, d, q) model, the term d denotes the order of difference g. An ARIMA model with order of differencing d can be expressed as [4]:

$$\phi(B)(1-B)^d x_t = \theta(B)e_t \tag{9}$$

B. Neural Network Model

Neural networks (NN) for forecasting have been investigated by many researchers over past several years. The motivation for using neural networks is based on the fact that these 24 dels are capable of handling non-linear relationships. Examples of neural networks used for time series forecasting purposes can be found in [5, 6, 7, 8].

Neural Network model consists of different layers which are connected to each **21** r by connection weights. Between the extremities of the input layer and the output layer are the hidden layers. The nodes in each layer are connected by flexible weights, which are adjusted based on the error or bias.

The function of the input 21 er is for data entry, data processing takes place in the hidden layer and the output layer functions as the data output result. Fig. 1 shows the architecture of a general multilayer backpropagation neural network.

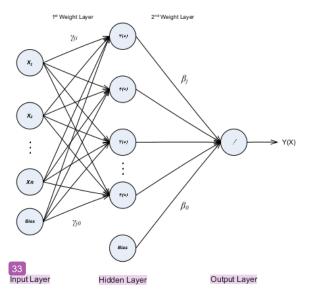


Figure 1. A general Multilayer Backpropagation Neural Network

In this architecture, the response value Y(x) is computed as [5]:

$$Y(x) = \beta_0 + \sum_{j=1}^{H} \beta_j \psi(\gamma_{j0} + \sum_{j=1}^{n} \gamma_{ji} x_i)$$
(10)

where $(\beta_0, \beta_1, ..., \beta_H, \gamma_{10},..., \gamma_{Hn})$ are the weights or parameters of the Neural Network. The non linearity enters into the function Y(x) through the so called activation function ψ .

Information processing in every neuron is done by summing the multiplication result of connection weights with input data. The result is transferred to the next neuron through the activation function. There are several kinds of activation functions ψ , such as sigmoid, bipolar sigmoid and hyperbolic tangent.

The Hyperbolic Tangent activation function [9] given below:

$$\psi(x_j) = \tanh(x_j) = \frac{e^{x_j} - e^{-x_j}}{e^{x_j} + e^{-x_j}}$$
(11)

(8)

C. Linear Regression

The regression model describes the mean of the normally distributed dependent variable Y as a function of the predictor or independent variable x [10]:

$$Y_i = \beta_0 + \beta_i \mathbf{x}_i + \varepsilon_i \tag{12}$$

where Y_i is the value of the response or dependent variable from the *i*-th pair 20₀ and β_i are the two unknown parameters, x_i is the value of the independent variable from the *i*-th pair, and ε_i is a random error term.

The predicted or estimated or fitted values of the regression model are calculated as [11]:

$$Y_i = b_0 + b_1 \mathbf{x}_i \tag{13}$$

The parameters b_0 and b_1 in the above equation are computed as:

$$b_{0} = \mu - \beta_{1} (n+1)/2$$

$$b_{1} = [\theta - n \mu (n+1)/2] / [\sigma^{2} - n (n+1)^{2}/4]$$
where
$$\mu = \sum_{i=1}^{n} x_{i} / n$$

$$\theta = \sum_{i=1}^{n} i . x_{i}$$

$$\sigma^{2} = \sum_{i=1}^{n} x_{i}^{2}$$
(14)

This mod \mathfrak{g} is referred to as the linear regression (LR) model [11]. It is linear because the independent variable appears only in the first power; if we plot the mean of Y versus x, the graph will be a straight line with intercept b_0 and slope b_L

D. Performance Measures

The prediction models are evaluated in terms of their ability to 49 recast the future values. Several measures are used in comparing forecastin 42 performance of different models. The most common measure is the Root M(15 Square Error (RMSE). The other measures that are used are the mean absolute error (MAE) and the mean absolute percentage error (MAPE).

The Root Mean Square Error and mean absolute percentage error are used for comparison of model accuracy. Lower values are better. The MAE measures the average magnitude of the error. The RMSE is likely to be used for 6 ta that has the undesirable large error. And both MAE and RMSE can be used together to diagnose the variation in the errors in a set of forecast. If value of RMS 6 > MAE then there is a variation in the errors. They are negativelyoriented scores. Lower values are better.

The three forecast error statistics are computed as follows:

1) Mean Absolute Error (MAE)

The MAE measures the average magnitude of the errors in a set of forecasts, without considering their direction. [12]:

$$MAE = \frac{\sum_{t=1}^{n} \left| Y_t - \hat{Y}_t \right|}{n} \tag{15}$$

2) Mean Absolute Percentage Error (MAPE)

MAPE produces a measure of relative overall fit [12]:

$$MAPE = \frac{\sum_{t=1}^{n} \frac{\left|Y_t - \hat{Y}_t\right|}{Y_t} * 100}{n}$$

3) Root Mean Square Error (RMSE)

The **RMSE** is a quadratic scoring rule which measures the average magnitude of the error. [12, 13]

$$\frac{\sum_{t=1}^{n} \left(Y_t - \hat{Y}_t\right)^2}{n}$$
(17)

(16)

III. DATA

The infant mortality rate data used in this study are collected in Indonesia from Indonesian Health Profile, Ministry of Health Republic of Indonesia. Table 1 shows the IMR data during 1995-2008.

Table 1. IMR in Indonesia during 1995-2008

NO	YEAR	IMR
1	1995	55.00
2	1996	54.00
3	1997	52.00
4	1998	50.00
5	1999	44.00
6	2000	47.00
7	2001	50.00
8	2002	35.00
9	2003	38.00
10	2004	36.00
11	2005	36.00
12	2006	34.00
13	2007	32.00
14	2008	31.00

The statistical features 40 the IMR data such as the minimum, maximum, mean, standard deviation and Variance are shown in Table 2.

Table 2. . Descriptive Statistics of IMR in Indonesia

Name	Min	Max	Mean	Std. Dev.	Variance
IMR	31.00	55.00	42.4286	8.72410	76.110

IV. RESULTS

In this section, we compare the three prediction models. The models are based on ARIMA, Neural Network and Linear Regression. The results achieved by each implemented model are discussed below.

A. ARIMA Model

We compute prediction using ARIMA models with different parameter (p, d, q) values. The result of the time series forecasting with different ARIMA models is shown in Table 3.

	the time	series	forecasting	with ARIMA
4.4				

		11						
Year	Actual	ARIMA	ARIMA	ARIMA	ARIMA	ARIMA	ARIMA	ARIMA
rear	Data	(1,0,0)	(0, 0, 1)	(1,0,1)	(0,1,1)	(1,1,0)	(1,1,1)	(0,1,0)
1995	55	42.62	42.42	42.94				
1996	54	53.40	48.14	53.60	53.00	53.11	53.01	53.15
1997	52	52.53	45.78	53.10	51.49	51.72	51.44	52.15
1998	50	50.79	46.25	51.54	49.66	50.16	49.66	50.15
1999	44	49.05	44.79	49.78	47.74	48.16	47.76	48.15
2000	47	43.82	41.92	45.06	44.99	43.92	45.64	42.15
2001	50	46.43	45.68	46.32	43.32	42.96	43.07	45.15
2002	35	49.05	45.20	48.75	42.27	45.96	41.29	48.15
2003	38	35.98	35.87	38.29	39.36	38.89	40.63	33.15
2004	36	38.60	43.79	38.42	37.20	33.96	37.52	36.15
2005	36	36.85	37.41	36.99	35.08	34.16	35.38	34.15
2006	34	36.85	41.51	36.71	33.16	33.28	33.12	34.15
2007	32	35.11	37.59	35.20	31.22	32.16	31.21	32.15
2008	31	33.37	38.83	33.44	29.28	30.16	29.29	30.15
2009		32.50	37.39	32.37	27.40	28.72	27.26	29.15
MAE		3.853	5.790	3.737	2.183	2.543	2.184	2.781
MAPE		8.452	13.591	9.135	5.412	6.334	5.413	7.013
RMSE		6.022	7.133	6.176	3.375	4.337	3.450	4.705

From Table 3, it is noted that the smalles $\frac{127}{100}$ lues of MAE, MAPE and RMSE are obtained for the model ARIMA(0,1,1). So, we can conclude that ARIMA(0,1,1) is the best ARIMA model.

Fig. 2 illustrates the a 2 al and predicted graph of ARIMA models, where the horizontal axis represents the time (year) and the vertical axis is the value of IMR.

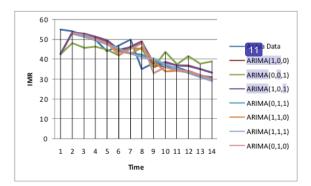


Figure 2. The actual and prediction graph of ARIMA Model

B. Neural Network Model

We also computed prediction using a multi-layer perceptron Neural Network model. Architecture configurations with different numbers of input and hidden layer neurons were tested to determine the optimum setup. Similarly, different activation functions such as hyperbolic Bygent, bipolar sigmoid and sigmoid functions were tested. From the experimental realits, it is found that the neural network model with 6 input neuron 4 10 hidden layer neurons and using hyperbolic tangent activation functions for the hidden and output layers yields the minimum values for MAE, MAPE and RMSE.

Year	Actual Data	FORECASTING NO. OF INPUT NEURONS					
		6	5	4	3	2	1
1995	55						
1996	54						50.10
1997	52					52.24	49.63
1998	50				47.87	48.77	48.58
1999	44			43.62	47.04	43.22	47.36
2000	47		47.19	47.54	45.73	47.38	42.64
2001	50	49.53	49.66	49.52	50.22	46.94	45.20
2002	35	35.28	35.17	35.55	35.01	38.85	47.36
2003	38	38.04	37.90	37.86	38.43	38.72	34.50
2004	36	36.20	36.11	36.33	35.67	37.66	36.95
2005	36	36.09	35.97	35.57	34.87	34.41	35.26
2006	34	34.17	33.96	32.08	33.91	33.89	35.26
2007	32	32.02	31.41	32.64	32.93	31.63	33.82
2008	31	30.42	31.62	32.30	31.57	30.53	32.69
2009		31.73	31.48	32.45	31.11	30.25	32.23
MAE		0.234	0.242	0.672	0.923	1.204	3.271
MAPE		0.395	0.474	1.453	1.560	2.583	6.967
RMSE		0.300	0.322	0.842	1.287	1.649	4.389
48							

172 results of the time series forecasting using the optimum Neural Network model are shown in Table 4. For the sake of comparison, the results obtained for the different number of input neurons are also shown in Table 4.

Fig 3. Illustrates the actual and predicted graph of the optimum Neural Network models, where the horizontal axis represents the time (year) and the vertical axis is the value of IMR.

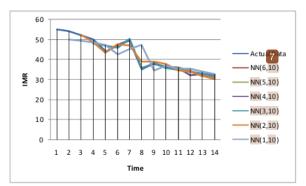


Figure 3. The actual and prediction graph of Neural Network Model

C. Linear Regression

The Linear Regression model for time series forecasting is obtained as follows:

$Y_i = 57.198 - 1.969 i$

where Y_i is the predicted value for i-th year.

The result of the time series forecasting with Linear Regression model is shown in Table 5.

Table 5. Result of the time series forecasting with Linear Regression

(18)

Year	Actual Data	FORECASTING
1995	55	55.23
1996	54	53.26
1997	52	51.29
1998	50	49.32
1999	44	47.35
2000	47	45.38
2001	50	43.41
2002	35	41.44
2003	38	39.47
2004	36	37.51
2005	36	35.54
2006	34	33.57
2007	32	31.60
2008	31	29.63
2009		27.66
MAE		1.858
MAPE		4.533
RMSE		2.767

Fig 4. Illustrates the actual a 21 predicted graph of Linear Regression model where the horizontal axis represents the time (year) and the vertical axis is the value of IMR.

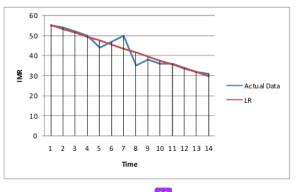


Figure 4. The actual and pre 39 ion graph of Linear Regression Model

D. Comparison of Models

Table 6 shows the comparison of MAE, MAPE and RMSE obtained with ARIMA, Neural Network and Linear Regression models.

From Table 6, it is seen that the best model for the predicti 19 of Infant Mortality Rate is the Neural Network Model with 6 input neurons, 10 hidden layer neurons (NN(6, 10)) using hyperbolic tangent activation functions

Table 6. Performance Measure of Models

MODELS	PERFORMANCE MEASURE				
11 MODELS	MAE	MAPE	RMSE		
ARIMA(1,0,0)	3.853	8.452	6.022		
ARIMA(0,0,1)	5.790	13.591	7.133		
ARIMA(1,0,1)	3.737	9.135	6.176		
ARIMA(0,1,1)	2.183	5.412	3.375		
ARIMA(1,1,0)	2.543	6.334	4.337		
ARIMA(1,1,1)	2.184	5.413	3.450		
ARIN.7.(0,1,0)	2.781	7.013	4.705		
NN(6,10)	0.234	0.395	0.300		
NN(5,10)	0.242	0.474	0.322		
NN(4,10)	0.672	1.453	0.842		
NN(3,10)	0.923	1.560	1.287		
NN(2,10)	1.204	2.583	1.649		
NN(1,10)	3.271	6.967	4.389		
LR	1.858	4.533	2.767		

Fig.5 compares the per2 mance measures of different models graphically. The horizontal axis represents the models and the vertical axis is the values of performance measure.

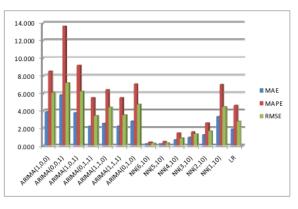


Figure 5. Comparison performance measure of models

V. CONCLUSION

This paper has described three prediction models for Infant Mortality Rate. The prediction was done using ARIMA, Neural Network and Linear Regression models. The performances of the models are compared using the data of Infant Mortality Rate collected during 1995 – 2008 in Indo 28 ia. Performance measures such as Mean Absolute Error, Mean Absolute Percentage Error and Root Mean Square 38 pr have been employed for comparison. From the 19 ults, it was found that the Neural Network model with 6 input neurons, 10 4 urons in the hidden layer and using hyperbolic tangent activation functions for the hidden and output layers yields the best forecasting result.

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